



**JARAMOGI OGINGA ODONGA UNIVERSITY  
OF SCIENCE AND TECHNOLOGY**

**FIRST YEAR SECOND SEMESTER EXAMINATION FOR THE DEGREE OF  
BACHELOR OF SCIENCE -DECEMBER 2020**

**SMA 3121: MATHEMATICS II (SPECIAL EXAM)**

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**INSTRUCTIONS:**

1. This examination paper contains five questions. Answer **question one**, and **any other two** questions.
2. Start each question on a fresh page.
3. Indicate question number clearly at the top of each page.

**QUESTION ONE (COMPULSORY) (30 MARKS)**

- a) Given two matrices  $A = \begin{bmatrix} 2 & 1 \\ 3 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & -2 \\ 1 & 2 \end{bmatrix}$ . Find
- i.  $2A-3B$  (2 marks)
  - ii.  $BA$  (2 marks)
  - iii.  $B^{-1}$  (3 marks)
- b) Given two points P(0, -1) and Q(4, 1). Find the equation of the line that is perpendicular to PQ and passes through the midpoint of PQ. (4 marks)
- c) Evaluate
- i)  $\lim_{x \rightarrow 1} (x^2 + 1)$  (2 marks)
  - ii)  $\lim_{x \rightarrow 3} (x^2 + x + 6)$  (3 marks)
- d) Determine the area between the curve  $y = x^3 - 2x^2 - 8x$  and x-axis. (5 marks)
- e) Find  $\frac{dy}{dx}$  in  $x^2 - y^2 = 1$ . (3 marks)

- f) Consider the three points A(-2,1) B(2,3) and C(3,1).
- i) Find the length of each side of the triangle. (3 marks)
  - ii) Verify that the triangle is right angle triangle (2 marks)
  - iii) Find the area of the triangle. (1 mark)

**QUESTION TWO (20 MARKS)**

a) Given the matrix  $A = \begin{bmatrix} 1 & 2 & -1 \\ 3 & 0 & 1 \\ 4 & 2 & 1 \end{bmatrix}$ . Find

- i)  $|3A|$  (2 marks)
  - ii) The adjoint of A. (4 marks)
  - iii) Inverse of A. (3 marks)
- b) Solve the system of equations using Cramers rule (6 marks)
- $$x_1 + 3x_2 + x_3 = -2$$
- $$2x_1 + 5x_2 + x_3 = -5$$
- $$x_1 + 2x_2 + 3x_3 = 6$$

c) Evaluate  $\int 3te^{2t} dt$  (5 marks)

**QUESTION THREE (20 MARKS)**

- a) Find the derivative of the polynomial
- i)  $y = x^3 + \frac{4}{3}x^2 - 5x + 1$  (3 marks)
  - ii)  $y = \frac{x^2 - 1}{x^3 + 1}$  (3 marks)

b) Determine if the following functions are continuous or discontinuous.

- i)  $f(x) = \frac{3x^2 - 7x + 2}{x - 2}$  (3 marks)
- ii)  $f(x) = \frac{1}{x^2 + 1}$  (3 marks)

c) The concentration C in mg of a chemical in bloodstream t hours after injection into the muscle tissue can be modeled by  $C = \frac{3t}{27 + t^3}; t \geq 0$ . Determine the time when the concentration reaches its highest level. (5 marks)

d) Find the distance between A(1,1) and B(3,4). (3 marks)

**QUESTION FOUR (20 MARKS)**

- a) Use Gauss-Jordan elimination to solve (6 marks)  
 $3x - y = 7$   
 $2x + 5y = 16$
- b) Find  $\frac{dy}{dx}$  if  $2x^3 - 3y^2 = 8$  (6 marks)
- c) Find the slope  $m$  and  $y$ -intercept of the equation  $2x+4y=8$ . (3 marks)
- d) Solve the following equation for the variable  $x$   $\begin{vmatrix} x & x+1 \\ -1 & x-2 \end{vmatrix} = 7$ . (5 marks)

**QUESTION FIVE (20 MARKS)**

- a) Evaluate the given definite integral (5 marks)  
$$\int_{-1}^0 (-3x^5 - 3x^2 + 2x + 5)dx$$
- b) Given a system of equations  
 $2x_1 + 7x_2 + 3x_3 = 7$   
 $x_1 + 2x_2 + x_3 = 2$   
 $x_1 + 5x_2 + 2x_3 = 5$
- (i) Express the system in the form of matrix equation  $AB = C$ , where  $A$  is a  $3 \times 3$  matrix of coefficients of the variables,  $B$  and  $C$  are suitable column matrices. (2 marks)
- (ii) Determine the adjoint of the matrix  $A$ . (5 marks)
- (iii) Hence solve the system of equations. (4 marks)
- c) Does the curve  $y = x^4 - 2x^2 + 2$  have any horizontal tangent? If so where? (4 marks)