

# JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE AND TECHNOLOGY

# SCHOOL OF MATHEMATICS AND ACTUARIAL SCIENCE

# UNIVERSITY EXAMINATION FOR DEGREE OF BACHELOR OF EDUCATION AND ACTUARIAL SCIENCE

## 2022/2023 ACADEMIC YEAR

## MAIN CAMPUS

## **COURSE CODE: WAB 2109**

## COURSE TITLE: INTRODUCTION TO PROBABILITY THEORY

**EXAM VENUE:** 

STREAM: ACTUARIAL SCIENCE

DATE:

**EXAM SESSION:** 

#### TIME: 2.00 HOURS

Instructions:

- 1. Answer question one (compulsory) and any other two questions.
- 2. Candidates are advised not to write on the question paper.
- **3.** Candidates must hand in their answer booklets to the invigilator while in the examination room.

## **Question One Compulsory (30mks)**

- a) Briefly explain the meaning of the following terms as used in Probability (8marks)
  - i) Sample Space
  - ii) Sample Point
  - iii) Probability
  - iv) Exhaustive Events
- b) If  $A^{C}$  is the complement of event A, prove that  $P(A^{C}) = 1 P(A)$  (5marks)
- c) The Probability that John passes a Maths exam is 4/5 and that he passes a Chemistry exam is 5/6. If the probability that he passes both exams is 3/4, find the probability that he will pass at least one exam. (5marks)

- d) In a large metropolitan area, the probability of a family owning a colour T.V, a computer or both 0.86, 0.35 and 0.29 respectively. What is the probability that a family chosen at random during a survey will own a colour T.V and/or a computer? Given that the family chosen at random during a survey owns a colour T.V, what is the probability that it will own a computer? (5marks)
- e) A group of 50 people was asked which of the three novels they read A, B or C. the results showed that 25 read A, 16 read B, 14 read C, five read both A and C while 2 read all the three. If a person is chosen at random from these group, find the probability that he

i)	Reads A only	(2marks)
ii)	Reads only one of the novels	(2marks)
iii)	Read at least one of the novels	(3marks)

#### Question Two (20mks)

a) At a certain assembly plant, three machines make 30%, 45%, and 25%, respectively, of the products. It is known from the past experience that 2%, 3% and 2% of the products made by each machine, respectively, are defective. Now, suppose that a finished product is randomly selected.
i) What is the probability that it is defective?

i)What is the probability that it is defective? (5marks)ii) If a product were chosen randomly and found to be defective, what is the probability that it was made by machine 3? (5marks)

b) Of the customers at a gas station, 70% use regular gas, and 30% use diesel. Of the customers who use regular gas, 60% will fill the tank completely, and of those who use diesel, 80% will fill the tank completely.

i)What percent of all customers will fill the tank completely? (5marks)ii) If a customer has filled up completely, what is the probability it was a customer buying diesel? (5marks)

#### **Question Three (20mks)**

a) Let X be a random variable with PDF given by  $f_x(x) = \begin{cases} cx^2 & x \le 1\\ 0, otherwise \end{cases}$ i) Find the constant c. (4marks) ii) Find E(X) and Var(X). (6marks)

iii) Find 
$$P(X \ge \frac{1}{2})$$
 (4marks)

$$f_{X}(x) = \begin{cases} 4x^{3} & 0 < x \le 1\\ 0, otherwise \end{cases}$$
  
Find P(X $\le \frac{2}{3}$ |X> $\frac{1}{3}$ ) (6marks)

#### **Question Four (20mks)**

Let X be a discrete random variable with the following PMF  $c_{0,1}$  for x = 0.2

$$PX(x) = \begin{cases} 0.1 & for \ x = 0.2 \\ 0.2 & for \ x = 0.4 \\ 0.2 & for \ x = .05 \\ 0.3 & for \ x = 0.8 \\ 0.2 & for \ x = 1 \\ otherwise \end{cases}$$

c)	Find RX, the range of the random variable X.	(5marks)
d)	Find $P(X \le 0.5)P(X \le 0.5)$ .	(5marks)
e)	Find P(0.25 <x<0.75)< td=""><td>(5marks)</td></x<0.75)<>	(5marks)
f)	Find P(X=0.2 X<0.6).	(5marks)

#### **Question Five (20mks)**

You take an exam that contains 20 multiple-choice questions. Each question has 4 possible options. You know the answer to 10 questions, but you have no idea about the other 10 questions so you choose answers randomly. Your score X on the exam is the total number of correct answers. i)Find the PMF of X. (10marks) (10marks)

ii)What is P(X>15)

(5marks)