JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE AND TECHNOLOGY SCHOOL OF BIOLOGICAL PHYSICAL MATHEMATICS AND ACTUARIAL SCIENCE<br>UNIVERSITY EXAMINATION FOR DEGREE OF BACHELOR OF SCIENCE ACTUARIAL, B.ed SCIENCE, B.ed ARTS, B.ed SPECIAL NEEDS<br>$1^{\text {ST }}$ YEAR $1^{\text {ST }}$ SEMESTER 2022/2023 ACADEMIC YEAR<br>REGULAR (MAIN)

COURSE CODE: WAB 2107
COURSE TITLE: DESCRIPTIVE STATISTICS
EXAM VENUE:

DATE:
TIME: 2.00 HOURS

## Instructions:

1. Answer question 1 (Compulsory) and ANY other 2 questions
2. Candidates are advised not to write on the question paper.
3. Candidates must hand in their answer booklets to the invigilator while in the examination room.

## QUESTION ONE (30 MARKS)

a) Outline FOUR uses of statistics
b) The speeds, to the nearest mile per hour of 120 vehicles passing a check point were recorded and are grouped in the table below

| Speed in km/hour | $21-25$ | $26-30$ | $31-35$ | $36-45$ | $46-60$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of vehicles | 22 | 48 | 25 | 16 | 9 |

Estimate the mean speed of the vehicles
c) Cartons of orange juice are advertised as containing one liter. A random sample of 100 cartons gave the following results for the volume of $x$.

$$
\sum x=101.4 \quad \sum x^{2}=102.83
$$

Calculate the mean and standard deviation of the volume of orange juice in 100 cartons. (3 Marks)
d) 31 students tried to estimate the length of a line. The line was actually 60 mm long. These are their results in millimeters

| 61 | 70 | 46 | 44 | 26 | 23 | 30 | 83 | 52 | 44 | 38 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 37 | 49 | 59 | 58 | 63 | 31 | 29 | 37 | 48 | 76 | 61 |
| 46 | 31 | 38 | 41 | 49 | 52 | 56 | 75 | 61 |  |  |

i. Find the median and the quartiles of this distribution and use the quartiles to estimate skewness.
ii. Draw a histogram with equal intervals $20 \leq l \leq 30 ; 30 \leq l \leq 40 ; \ldots$. (3 Marks)
e) An analysis of daily wages paid to workers in two factories A and B belonging to the same industry give the following information.

| Factory | A | B |
| :--- | :---: | :---: |
| No. of workers | 600 | 700 |
| Average daily wages | 286 | 275 |
| Variance of distribution | 81 | 100 |

i. Which factory is more consistent in wages.
(3 Marks)
ii. Find the average monthly wages of the workers in the two firms taken together.
iii. Find the combined variance of the two factories.
(3 Marks)
f) Outline THREE shortcomings of index numbers.

## QUESTION TWO (20 MARKS)

a) The first four moments of a distribution about the value 4 of the variable are $-1.5,17,-30$ and 108. Find the moment about mean.
(6 Marks)
b) Use the data below to calculate:
i. Quartile deviation
ii. Median
iii. Arithmetic mean (Take $A=45$ )
iv. Standard deviation
v. Coefficient of variation

| Class | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 20 | 12 | 10 | 8 | 5 |

(14 Marks)

## QUESTION THREE (20 MARKS)

a) Calculate the first four moments of the following distribution about the mean

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 1 | 8 | 18 | 46 | 70 | 46 | 18 | 8 | 1 |

(15 Marks)
b) Measure the coefficient of skewness and comment on the results.
(2 Marks)
c) Find the measure of kurtosis and comment on your results

## QUESTION FOUR (20 MARKS)

a) Outline TWO uses of index numbers.
(2 Marks)
b) Determine the Fisher price index for Year 0, Year 1 and Year 2 using year 0 as the base year from the table below.
(18 Marks)

|  | Year 0 |  | Year 1 |  | Year 2 |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Price | Quantity | Price | Quantity | Price | Quantity |
| Item A | 2 | 15 | 2.25 | 20 | 2.35 | 23 |
| Item B | 1 | 20 | 1.10 | 20 | 1.14 | 25 |
| Item C | 1.5 | 25 | 2.10 | 17 | 2.40 | 14 |

## QUESTION FIVE (20 MARKS)

a) Find the Pearson's correlation coefficient from the following table.

| $x$ | 1 | 3 | 4 | 6 | 8 | 9 | 11 | 14 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 1 | 2 | 4 | 4 | 5 | 7 | 8 | 9 |

(10 Marks)
b) In a partially destroyed laboratory, records of analysis of correlated dated had the following results that are found to be legible

Variance of $x=9$
Regression equation $8 x-10 y+66=0$

$$
40 x-18 y=214
$$

Find
i. the mean of $x$ and $y$
ii. the correlation coefficient between $x$ and $y$
iii. the standard deviation of $y$

