The aim at establishing the relationship between norms of norm-attainable elementary operators and norms of elementary operators in a general Banach algebra setting