SCHOOL OF SPATIAL PLANNING AND NATURAL RESOURCE MANAGEMENT UNIVERSITY EXAMINATION FOR THE DEGREE OF BACHELOR OF ARTS IN PLANNING AND MANAGEMENT

YEAR I SEMESTER I 2023/2024 DECEMBER EXAMS

## MAIN UNIVERSITY EXAMINATION

| COURSE CODE: | APP 802 |
| :--- | :--- |
| COURSE TITLE: | QUANTITATIVE METHODS |
| STREAM: | MASTER IN PLANNING AND DESIGN |
| SCHOOL: | SCHOOL OF SPATIAL PLANNING AND NATURAL <br>  <br> RESOURCE MAMAGEMENT <br> ACADEMIC YEAR: |
| VENUE | $2023 / 2024$ |
| DATE: | TBD |
| TIME: | TBD |

## Instructions:

1. Answer QUESTION ONE and ANY OTHER TWOquestions
2. Candidates are advised not to write on the question paper.
3. Candidates must hand in their answer booklets to the invigilator while in the examination room

## QUESTION 1

Consider the following frequency tabulation of a sample of land parcels in a peri-urban area in Ha :

| $\boldsymbol{X}_{\boldsymbol{i}}($ Ha. $)$ | $\boldsymbol{f}_{\boldsymbol{i}}$ (Number) |
| :--- | :---: |
| $1.85-1.95$ | 2 |
| $1.95-2.05$ | 1 |
| $2.05-2.15$ | 2 |
| $2.15-2.25$ | 3 |
| $2.25-2.35$ | 5 |
| $2.35-2.45$ | 6 |
| $2.45-2.55$ | 4 |
| $2.55-2.65$ | 3 |
| $2.65-2.75$ | 1 |

a) Using the midpoints of the indicated ranges of $X$,
i) Calculate the mean parcel size in Ha .
ii) Calculate the median parcel size in Ha.
iii) Determine the mode of the frequency distribution.
b) Consider the following data, which are a sample of amino acid concentrations ( $\mathrm{mg} / 100 \mathrm{ml}$ ) in arthropod hemolymph: 240.6, 238.2, 236.4, 244.8, 240.7, 241.3, 237.9.
i) Determine the range of the data
ii) Calculate the "sum of squares" of the data.
iii) Calculate the variance of the data.
iv) Calculate the standard deviation of the data.

## QUESTION 2

Discuss the principles, typical application, data requirements and limitations of:
a) Cluster Analysis
b) Principal Component Analysis (PCA)

## QUESTION 3

a) Differentiate between the characteristics of qualitative and quantitative data
b) Discuss the following types of data and approaches in analysis:
i) Data on ratio scale
ii) Data on interval scale
iii) Data on ordinal scale

## QUESTION 4

Based on the normal distribution and the Standard Score ( $Z$ ), discuss:
a) Type I and Type II statistical errors in hypothesis testing
b) Long-term probabilities in hypothesis testing
c) Statistical power of tests

## QUESTION 5

The following computer-based analysis shows the demand for middles class housing in two separate towns A and B. The demand is classified as low or high for 92 respondents with additional data on mortgage prices. Discuss and interpret these results based on qualitative approach to data analysis.
(20 Marks)
Binary Logistic Regression: Demand versus Source, Price

| Link function | Logit |
| :--- | :--- |

Response Information

| Variable | Value | Count |  |
| :--- | :--- | :--- | :--- |
| Demand | Low | 70 | (Event) |
|  | High | 22 |  |
|  | Total | 92 |  |

Deviance Table

| Source | DF | Adj Dev | Adj Mean | Chi-Square | P-Value |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Regression | 2 | 7.574 | 3.787 | 7.57 | 0.023 |
| Price | 1 | 4.629 | 4.629 | 4.63 | 0.031 |
| Town | 1 | 4.737 | 4.737 | 4.74 | 0.030 |
| Error | 89 | 93.640 | 1.052 |  |  |
| Total | 91 | 101.214 |  |  |  |

## Model Summary

| Deviance | Deviance |  |
| :---: | :--- | :--- |
| $\mathbf{R - S q}$ | R-Sq(adj) | AIC |
| $7.48 \%$ | $5.51 \%$ | 99.64 |

## Coefficients

| Term | Coef | SE Coef | VIF |
| :--- | :--- | :--- | :--- |
| Constant | -1.99 | 1.68 |  |
| Price | 0.0250 | 0.0123 | 1.12 |
| Town |  |  |  |
| Town B | -1.193 | 0.553 | 1.12 |

Odds Ratios for Continuous Predictors

|  | Odds Ratio | 95\% CI |
| :--- | :--- | :--- |
| Price | 1.0253 | $(1.0010,1.0503)$ |

Odds Ratios for Categorical Predictors(Odds ratio for level A relative to level B)

| Level A | Level B | Odds Ratio | 95\% CI |
| :--- | :--- | :--- | :--- |
| Town |  |  |  |
| Town B | Town A | 0.3033 | $0.1026,0.8966)$ |

## Regression Equation

$\mathrm{P}($ Low $)=\exp \left(\mathrm{Y}^{\prime}\right) /\left(1+\exp \left(\mathrm{Y}^{\prime}\right)\right)$

## Town

Goodness-of-Fit Tests

| Test | DF | Chi-Square | P-Value |
| :--- | :--- | :--- | :--- |
| Deviance | 89 | 93.64 | 0.348 |
| Pearson | 89 | 88.63 | 0.491 |
| Hosmer-Lemeshow | 8 | 4.75 | 0.784 |

Observed and Expected Frequencies for Hosmer-Lemeshow Test

| Group | Event Probability <br> Range | Demand = Low |  | Demand = High |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Expected | Observed | Expected |  |
| 1 | $(0.000,0.580)$ | 4 | 4.4 | 5 | 4.6 |
| 2 | $(0.580,0.668)$ | 6 | 6.4 | 4 | 3.6 |
| 3 | $(0.668,0.714)$ | 6 | 6.3 | 3 | 2.7 |
| 4 | $(0.714,0.745)$ | 8 | 6.6 | 1 | 2.4 |
| 5 | $(0.745,0.780)$ | 8 | 6.9 | 1 | 2.1 |
| 6 | $(0.780,0.812)$ | 6 | 7.2 | 3 | 1.8 |
| 7 | $(0.812,0.838)$ | 8 | 8.3 | 2 | 1.7 |
| 8 | $(0.838,0.869)$ | 12 | 12.9 | 3 | 2.1 |
| 9 | $(0.869,0.941)$ | 10 | 9.1 | 0 | 0.9 |
| 10 | $(0.941,0.967)$ | 2 | 1.9 | 0 | 0.1 |

## Measures of Association

| Pairs | Number | Percent | Summary Measures | Value |
| :--- | :--- | :--- | :--- | :--- |
| Concordant | 1045 | 67.9 | Somers’ D | 0.38 |
| Discordant | 461 | 29.9 | Goodman-Kruskal Gamma | 0.39 |
| Ties | 34 | 2.2 | Kendall's Tau-a | 0.14 |
| Total | 1540 | 100.0 |  |  |

SN USEFUL FORMULAE

1. $\bar{X}=\frac{\sum_{i=1}^{n} X_{i}}{n}$ or $\bar{X}=\frac{\sum X_{i}}{n}$
2. $\bar{X}=\frac{\sum_{i=1}^{k} f_{i} X_{i}}{n}$
3. $\quad$ sample median $=X_{(n+1) / 2}$.
4. $\quad$ median $=\binom{$ lower limit }{ of interval }$+\left(\frac{0.5 n-\text { cum. freq. }}{\text { no. of observations in interval }}\right)\binom{$ interval }{ size }
5. $\quad$ sample range $=$ largest $X-$ smallest $X$.
6. sample $\mathrm{SS}=\sum X_{i}^{2}-\frac{\left(\sum X_{i}\right)^{2}}{n}$
7. sample $\mathrm{SS}=\sum f_{i} X_{i}^{2}-\frac{\left(\sum f_{i} X_{i}\right)^{2}}{n}$
8. $s^{2}=\frac{\sum\left(X_{i}-\bar{X}\right)^{2}}{n-1}$.
9. $s^{2}=\frac{\sum X_{i}^{2}-\frac{\left(\sum X_{i}\right)^{2}}{n}}{n-1}$
10. $s=\sqrt{\frac{\sum X_{i}^{2}-\frac{\left(\sum X_{i}\right)^{2}}{n}}{n-1}}$.
