JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE AND TECHNOLOGY SCHOOL OF BUSINESS \& ECONOMICS

UNIVERSITY EXAMINATION FOR THE DEGREE OF BACHELOR OF BUSINESS
ADMINISTRATION WITH IT
$2^{\text {ND }}$ YEAR $1^{\text {ST }}$ SEMESTER 2019/2020 ACADEMIC YEAR
MAIN CAMPUS

COURSE CODE: AEC 205
COURSE TITLE: MANAGEMENT MATHEMATICS
EXAM VENUE:
STREAM: (BBA )
DATE:
EXAM SESSION:
TIME: 2 HOURS

## Instructions:

1. Answer Question ONE (COMPULSORY) and ANY other 2 questions
2. Candidates are advised not to write on the question paper.
3. Candidates must hand in their answer booklets to the invigilator while in the examination room.
1.(a) Given the matrices
$A=\left[\begin{array}{ll}1 & -4 \\ 0 & -9\end{array}\right]$
$B=\left[\begin{array}{cc}4 & 3 \\ -7 & 0\end{array}\right]$
$C=\left[\begin{array}{lll}5 & -1 & -1 \\ 12 & 0 & 2\end{array}\right]$

Calculate :
i. $\quad \mathrm{A}+4 \mathrm{~B}$
(4mks)
ii. $\quad(\mathrm{BC})^{\mathrm{T}}$
(4mks)
(b). Solve the following simultaneous equations by using matrix algebra

$$
\begin{gather*}
5 x+9 y=-30 \\
6 x-2 y=28 \tag{5mks}
\end{gather*}
$$

(c) Define markov chain and state the four conditions it must satisfy ( 5 mks )
(d) outline four purposes of input-output analysis
(e) A factory produces four products A, B, C and D which earns contribution of $£ 20, £ 25, £ 12$ and $£ 30$ per unit respectively. The factory employs 500 workers who work a 40 hour week. The hours required for each product and the material requirements are set out below:
products

|  | A | B | C | D |
| :--- | :--- | :--- | :--- | :--- |
| Hours per unit | 6 | 4 | 2 | 5 |
| Kg material x per unit | 2 | 8.3 | 5 | 9 |
| Kgs material y per unit | 10 | 4 | 8 | 2 |
| Kgs material z per unit | 1.5 | - | 2 | 8 |

The total availability of materials per week is:
X $\quad 100,000 \mathrm{~kg}$
Y $\quad 65,000 \mathrm{~kg}$
Z 250,000kg
The company wishes to maximize contribution
Formulate the L.P problem in the standard manner ( 4 mks )
$f(i)$ Calculate $d y / d x$ and $d y / d x^{2}$ for the following functions of $x$

$$
y=12-10 x+6 x^{2}-2 x^{3}
$$

2 (a) Affirm engaged in producing two models, model $\mathrm{x}_{1}$ and $\mathrm{x}_{2}$ performs only three operations -painting, assembly and testing. The relevant data are as follows:

| Unit sale price | Hours required for each unit |  |  |  |
| :--- | :--- | :--- | :--- | :---: |
|  | Assembly | Painting | Testing |  |
| Model $\mathrm{x}_{1}$ Rs 50 | 1.0 | 0.2 | 0.0 |  |
| Model $\mathrm{x}_{2}$ Rs 80 | 1.5 | 0.2 | 0.1 |  |

Total number of hours available each week is as under:

$$
\text { Assembly } 600
$$

Painting 100
Testing 30
The firm wishes to determine its weekly product mix so as to maximum revenue. Write up the model and then solve the product mix graphically.
(b) Solve the following simultaneous equations by using matrix algebra

$$
\begin{gather*}
\mathrm{X}_{1}+2 \mathrm{x}_{2}+\mathrm{x}_{3}=3 \\
2 \mathrm{x}_{1}+3 \mathrm{x}_{2}+2 \mathrm{x}_{3}=1 \\
3 \mathrm{x}_{1}+4 \mathrm{x}_{2}+\mathrm{x}_{3}=-2 \tag{10mks}
\end{gather*}
$$

3.(a) Write short notes on the following as used in markov analysis:
i. Transition probabilities
(2mks)
ii. Cyclic chains
(2mks)
iii. Steady states
(2mks)
iv. Absorbing states
(2mks)
v. Transient analysis
(2mks)
(b) Given the following transition matrix obtain the input -output matrix.

| Production sector | Purchase sector |  | Projected |
| :--- | :--- | :--- | :--- |
|  | Agriculture | Industry | Demand |
| Agriculture | 300 | 600 | 100 |
| Industry | 400 | 1200 | 400 |

If the projected demand changes to 200 and 800 units respectively, what should be the gross output of each sector in order to meet the new demands?
4. (a) Write short notes on the following:
i. Input-output tables
ii. Technical coefficients
iii. Final demands
iv. Leontief inverse matrix
(2mks)
(2mks)
(2mks)
(2mks)
b.i Solve the following simultaneous equations algebraically

$$
\begin{aligned}
& x+3 y=4 \\
& -x+2 y=6
\end{aligned}
$$

ii.intergrate (i) $x^{2}+1 / x^{2}$
(ii) $5 \mathrm{x}-3 \mathrm{x}^{2}$ (4mks)
5.(a) Determine the first, second and third derivatives of the following demand function.
i. $\quad \mathrm{P}=25 \mathrm{Q}^{4}-10 \mathrm{Q}^{2}+200$ (6mks)

Evaluate $\quad \lim _{x \rightarrow 1} \frac{x^{2}-1}{x-1}$
(b) A fast food chain has three shops, A, B and C. the average daily sales and profit in each shop is given in the following table:

|  | Units sold |  |  | Units profit |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | Shop A | Shop B | Shop C | Shop A | Shop B | Shop C |
| Burger | 800 | 400 | 500 | 20 p | 40 p | 33 p |
| Chips | 950 | 600 | 700 | 50 p | 45 p | 60 p |
| Drinks | 500 | 1200 | 900 | 30 p | 35 p | 20 p |

Use matrix multiplication to determine:
(a) The profit for each product
(b) The profit for each shop

